



SSEBop FANO Overview

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USGS EROS
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ET Estimation in Agriculture...

- It is a **RESPONSE** variable as opposed to precipitation (driver)
- It reflects the integrated effects of Energy/Aerodynamics, Soil Moisture, Vegetation and Environmental Stress

Potential

Energy

Wind/RH



Limitations

Moisture

Vegetation

Env. Stress



ET = Crop Water Use

Landsat 8

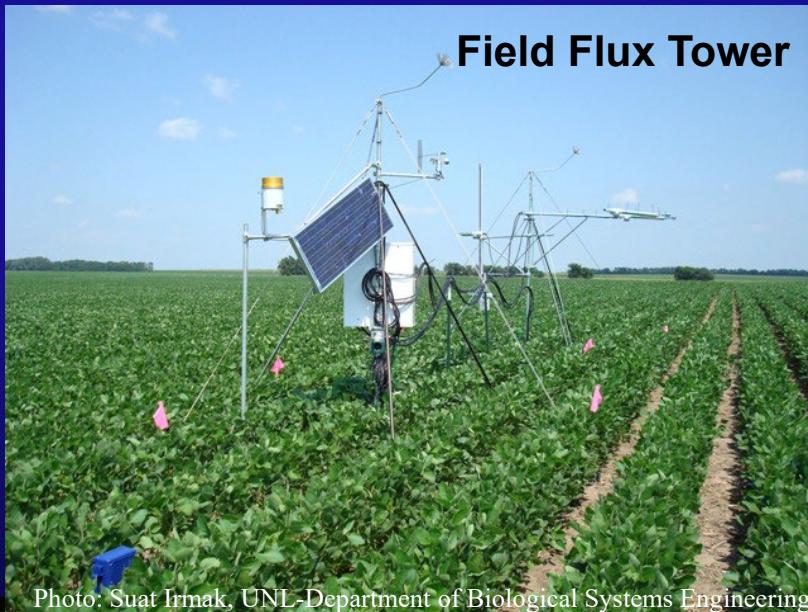


Photo: Suat Irmak, UNL Department of Biological Systems Engineering

**Evapotranspiration =
transpiration + evaporation**

$ET = \sim 70\% \text{ Precipitation}$

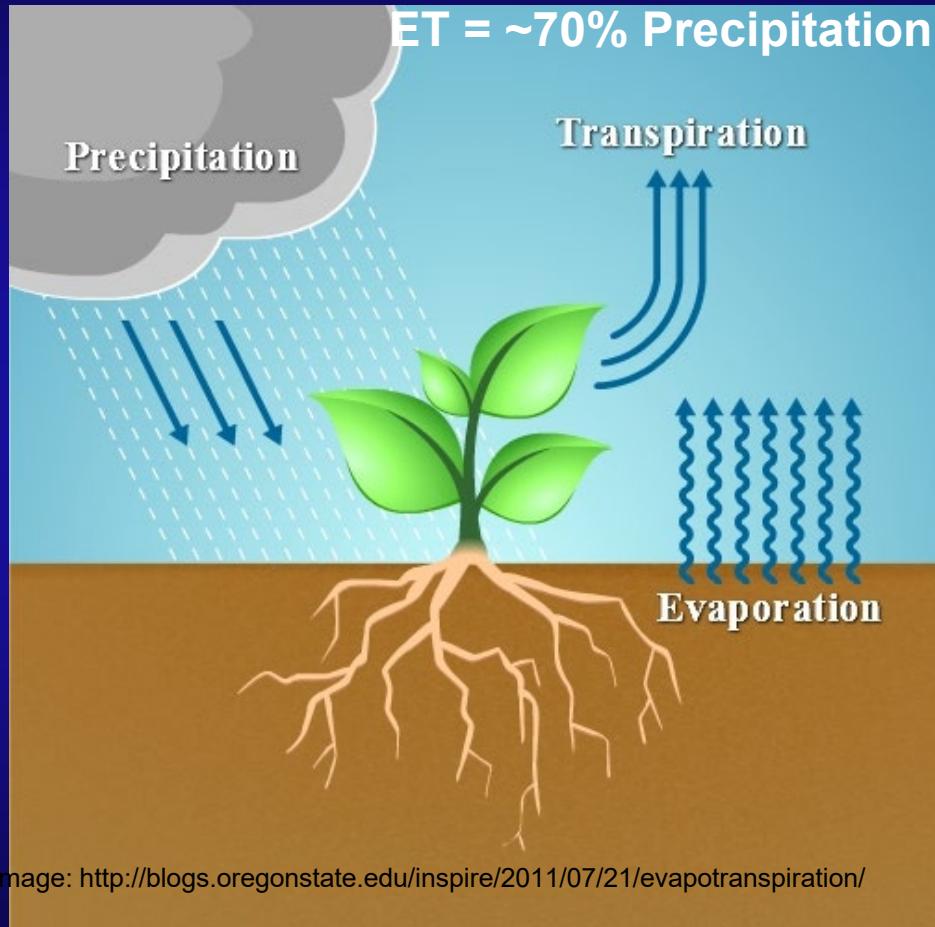
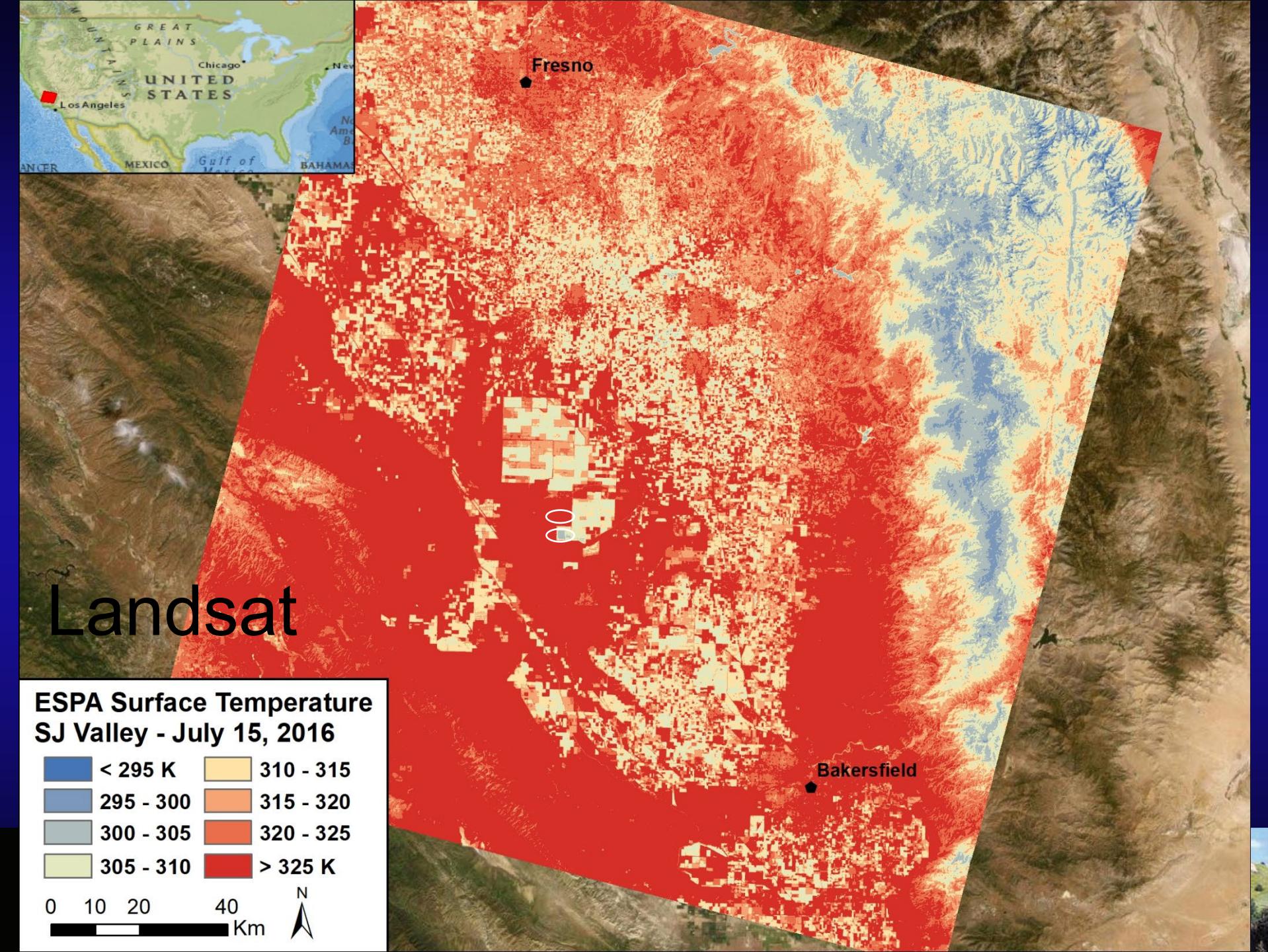
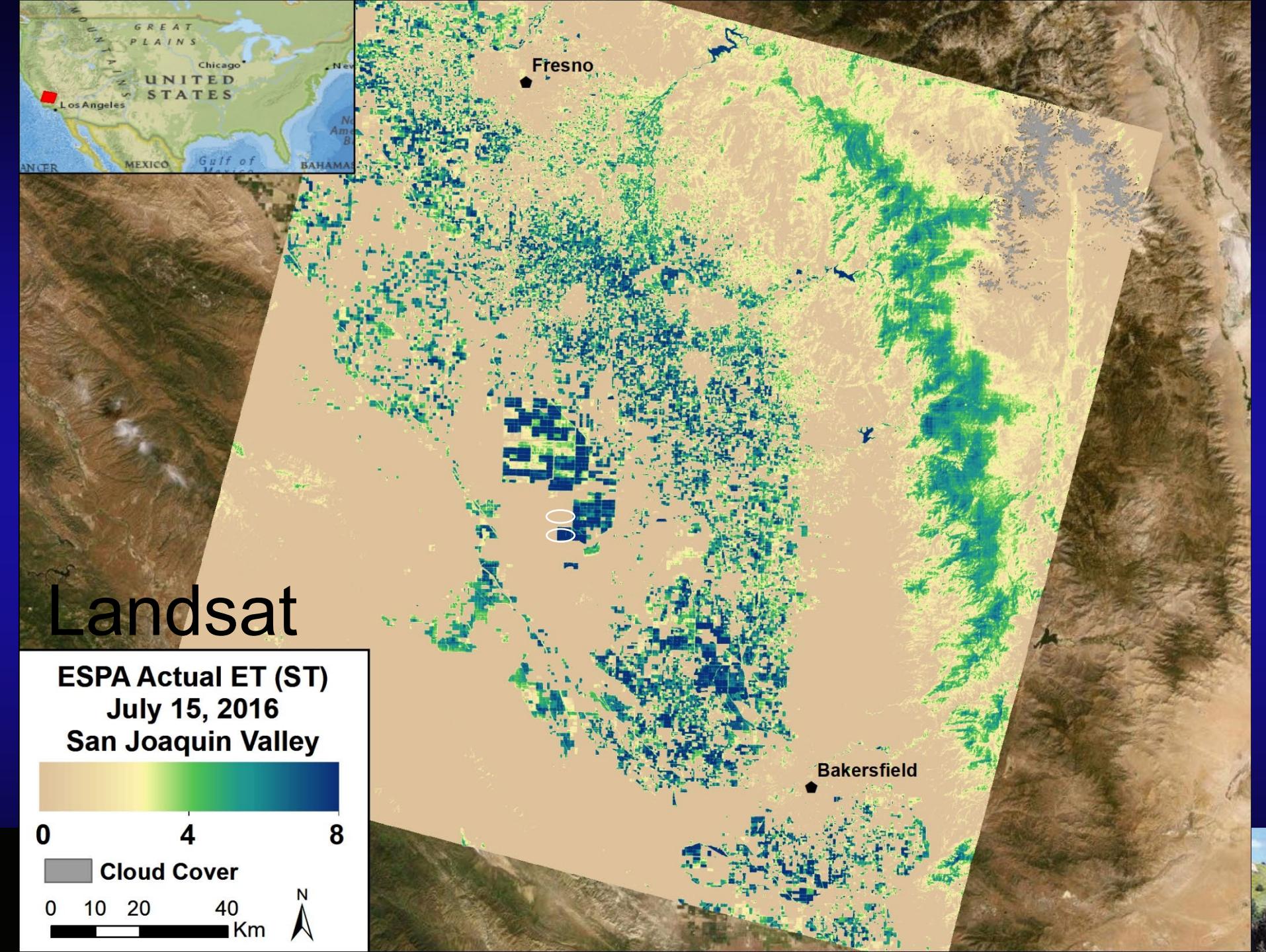


Image: <http://blogs.oregonstate.edu/inspire/2011/07/21/evapotranspiration/>



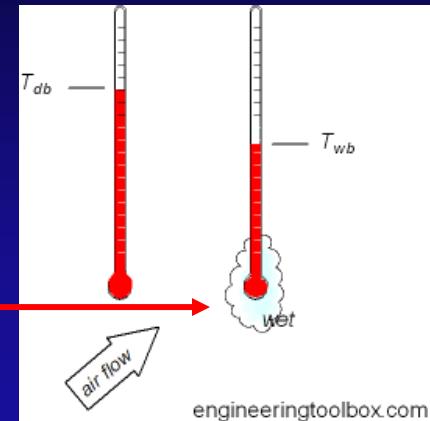


SSEBop Explained with “Psychrometry”

$$ea = es - \gamma (Td - Tw)$$

$$\gamma = \frac{C_p P}{\varepsilon \lambda} = 0.665 * 10^{-3} P$$

ea = actual vapor pressure (kPa)
es = saturated V.P. (kPa) at Tw



γ psychrometric constant [kPa $^{\circ}\text{C}^{-1}$]
P atmospheric pressure [kPa],
 λ latent heat of vaporization, 2.45 [MJ kg $^{-1}$]
 c_p specific heat of air at constant pressure,
1.013 10 $^{-3}$ [MJ kg $^{-1}$ $^{\circ}\text{C}^{-1}$]
 ε ratio molecular weight of water vapor/dry air
= 0.622.

Ferrel, W.M. (1886); Allen et al. (1998)

Air vs “Surface” Psychrometry (Thermometer vs Satellite Psychrometry)

Vapor pressure/relative humidity (standard psychrometry)

$$ea = es - \gamma (Td - Tw)$$

(Ferrel, W.M. (1886); Allen et al. (1998))

=> Large temp difference is a result of dry air (low RH) and hence low vapor pressure

Actual ET: Satellite “Psychrometry” Approach (SPA): SSEBop

$$ETa = ETo - \gamma^s (Ts - Tc) ETo$$

(Senay, 2018. App Eng. in Ag.)

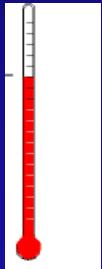
=> Large temperature difference is a result of dry soil/vegetation complex (low moisture, high stress) and hence low actual ET



Energy Balance Model: SSEBop



Land surface temperature differences are used to measure landscape water use rates through the effect of evaporative cooling



Surface Temp (T_s) 320 K

300 K
ET = Max



300 K

ET = moderate



310 K

ET = small



320 K

<http://www.croplife.com/equipment/>
irrigation-control-gets-ever-more-precise/

<https://www.irrigationaustralia.com.au/>
about-us/types-of-irrigation/drip-irrigation



Operational Simplified Surface Energy Balance (SSEBop)



parameters



Surface Temp (Ts)



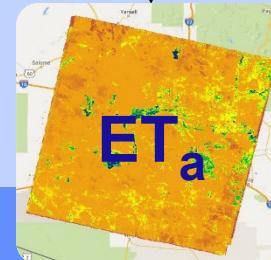
Weather Data

Radiation,
Temp, Wind,
RH, Pressure



Reference ET

ET fraction

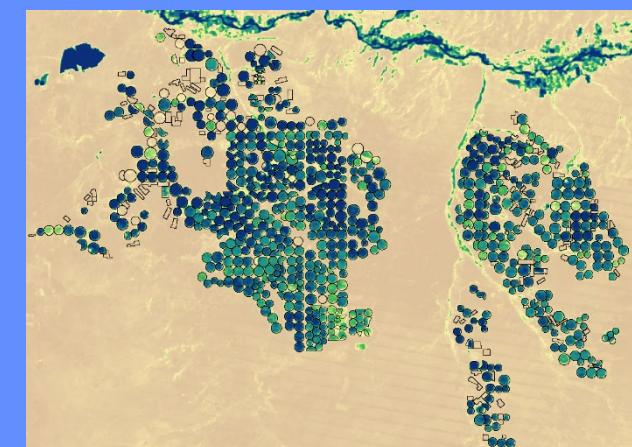


$$ET_a = ET_f * ETr$$

$$ET_f = 1 - \gamma^s(Ts - Tc)$$

$$\gamma^s = \frac{\rho \cdot C_p}{R_n \cdot r_{ah}}$$

$$Tc = Ts - f.dT(0.9 - NDVI): \text{FANO Equation (v6)}$$



Determining the Tc parameter

$$ET_f = 1 - \gamma^s(T_s - T_c)$$

- Satellite Psychrometry: the determination of the **wet-bulb**.
- Satellite acquires the ambient surface temperature (**dry-bulb**).
- We use the FANO Equation to determine Tc.



SSEBop: FANO

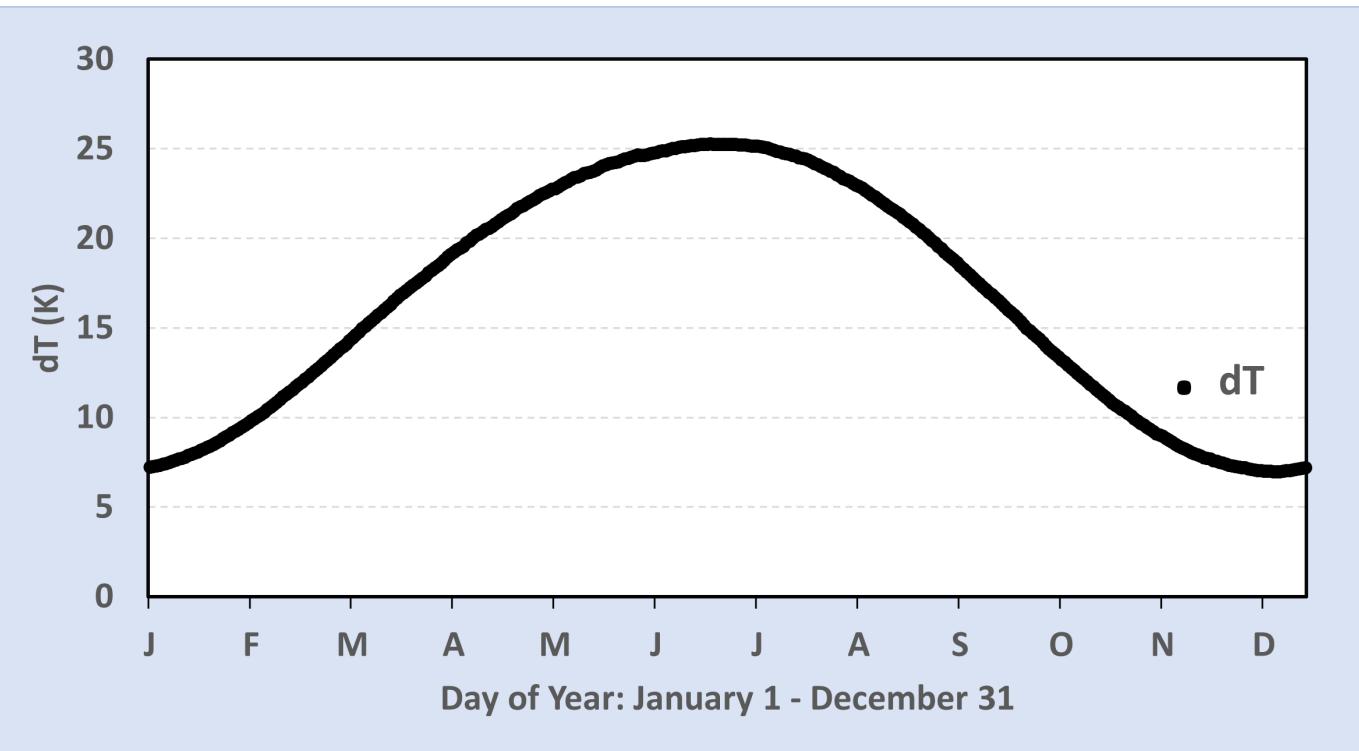
- A model parameterization approach using the **Forcing And Normalizing Operation**.
- **Forcing:** it forces the landscape to have a wet-bulb value for the boundary condition. This represents the land surface temperature at maximum ET.
- **Normalizing:** parameters are normalized to formulate the linear FANO equation.



dT ($1/\gamma^s$) parameter for SE Nevada

$$dT = \frac{R_n \cdot r_{ah}}{\rho \cdot C_p}$$

Input to the FANO Eqn.



dT : temperature difference [K, °C]
 R_n : Net radiation [$\text{MJ} \cdot \text{kg}^{-1} \cdot \text{d}^{-1}$]
 r_{ah} : aerodynamic resistance for heat [$\text{s} \cdot \text{m}^{-1}$]
 c_p : specific heat of air at constant pressure, $1.013 \cdot 10^{-3}$ [$\text{MJ} \cdot \text{kg}^{-1} \cdot {}^\circ\text{C}^{-1}$]

Kagone and Senay (2022)

Global dT is available at:

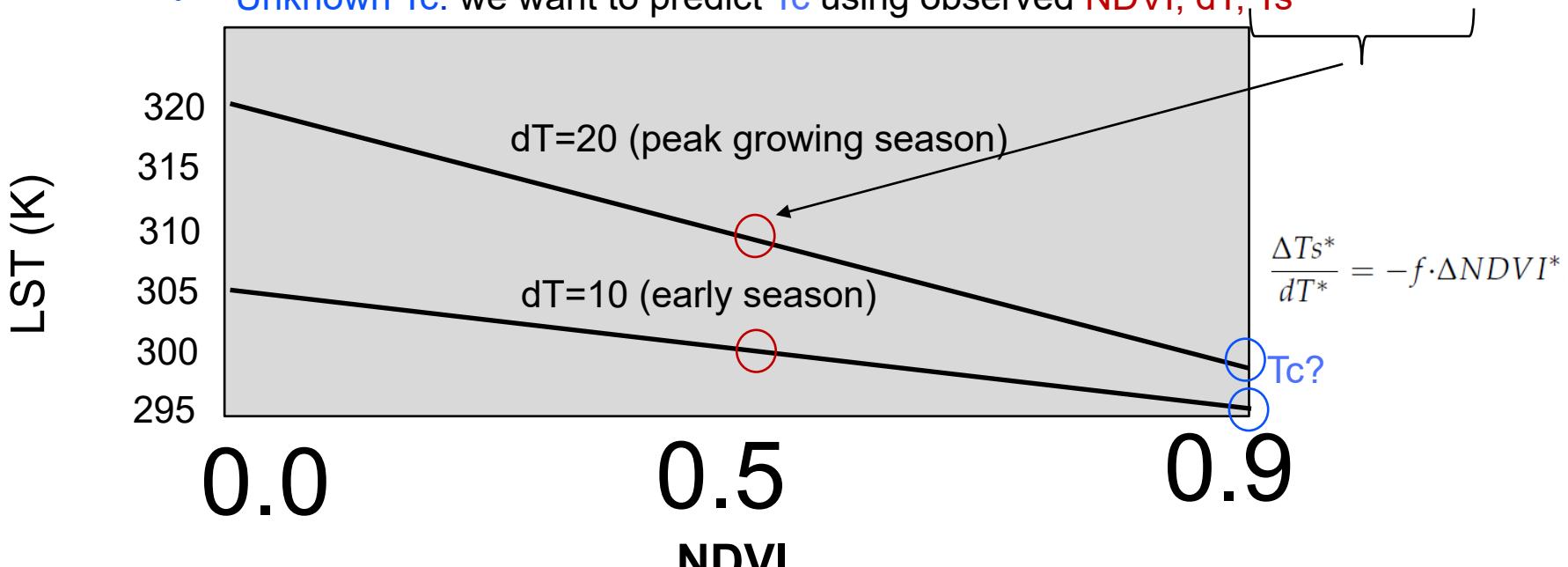
[Global gray-sky \$dT\$: the inverse of the surface psychrometric constant parameter in the SSEBop evapotranspiration model | U.S. Geological Survey \(usgs.gov\)](#)



Determining Tc using FANO Equation

Senay et al. (2023), RS.

- LST is inversely related to NDVI (“non-wet” landscapes)
- But degree (slope) of relation varies by season
- Normalizing by dT accounts for seasonal variation
- Maximum NDVI with maximum ET =~ 0.9 (assumed)
- Unknown Tc: we want to predict Tc using observed NDVI, dT, Ts



Same NDVI yields different Tc on different seasons.
Soln: Normalizing by dT

$$\Delta Ts^* = -f \cdot dT^* \cdot \Delta NDVI^*$$

$$\Delta NDVI^* = NDVI^* - NDVImax.$$

$$\Delta Ts^* = Ts^* - Tc^*.$$

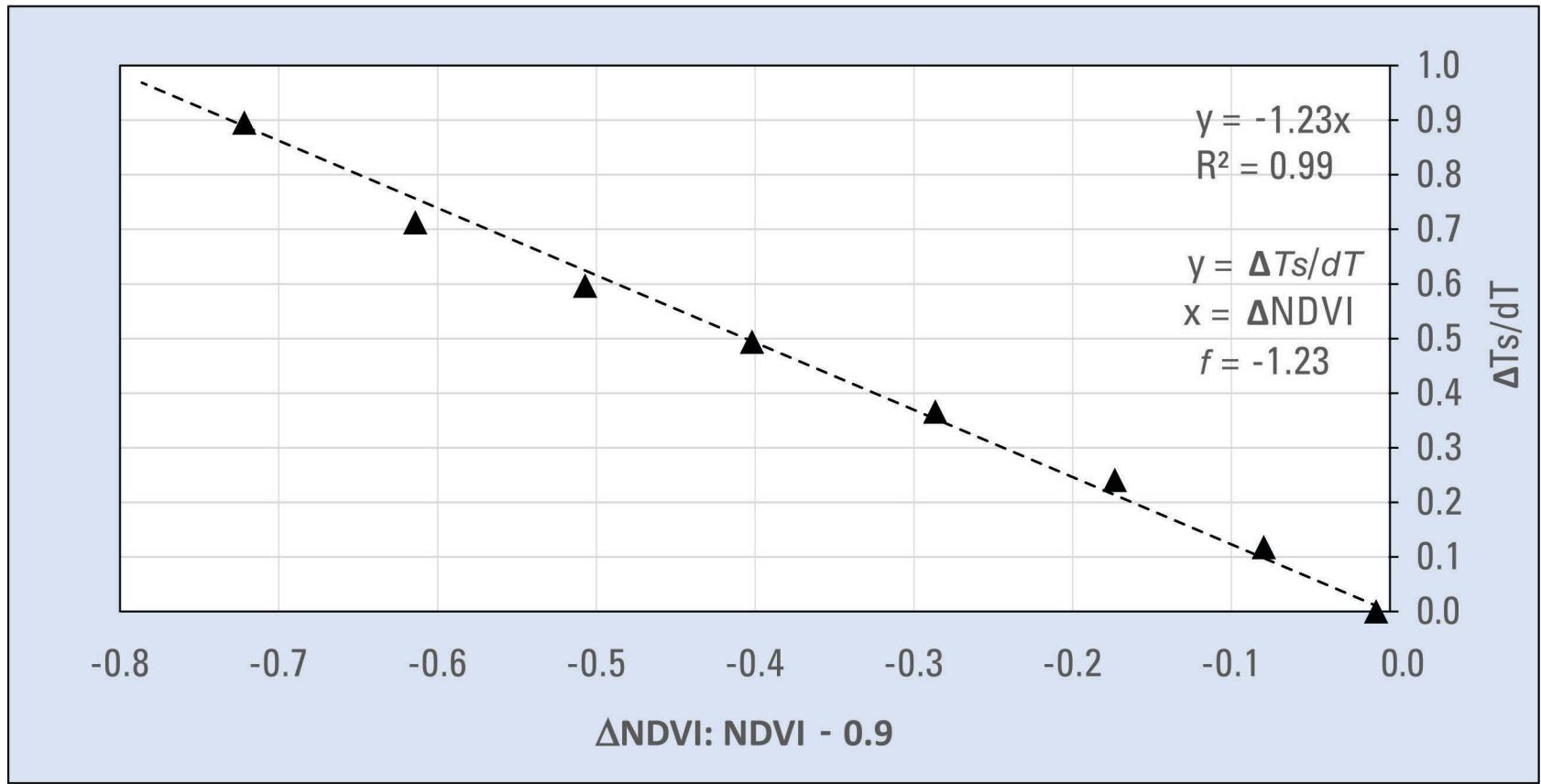


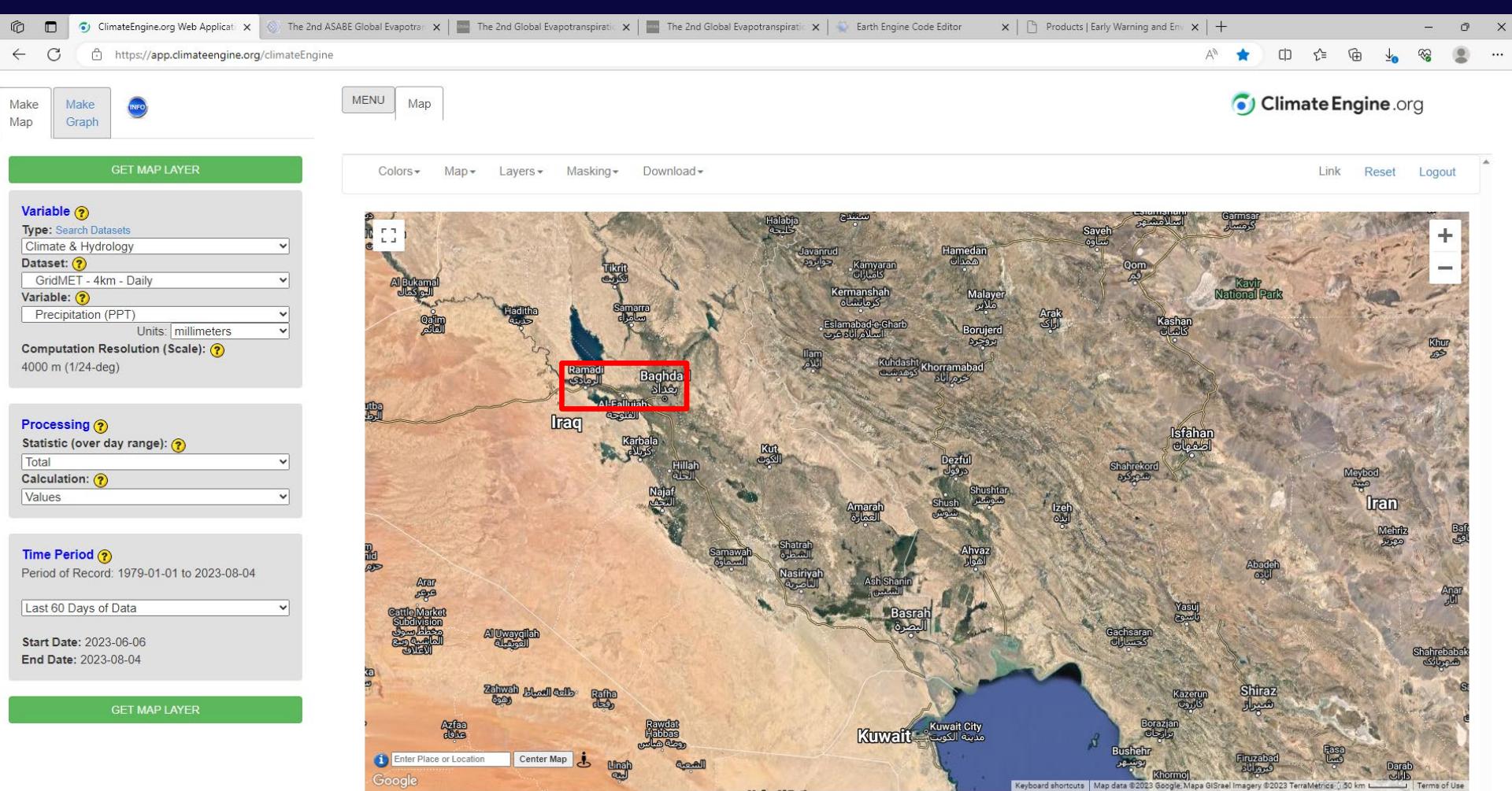
FANO Equation Formulation

$$\frac{\Delta Ts^*}{dT^*} = -f \cdot \Delta NDVI^*$$



$$Tc = Ts - f \cdot dT(0.9 - NDVI)$$





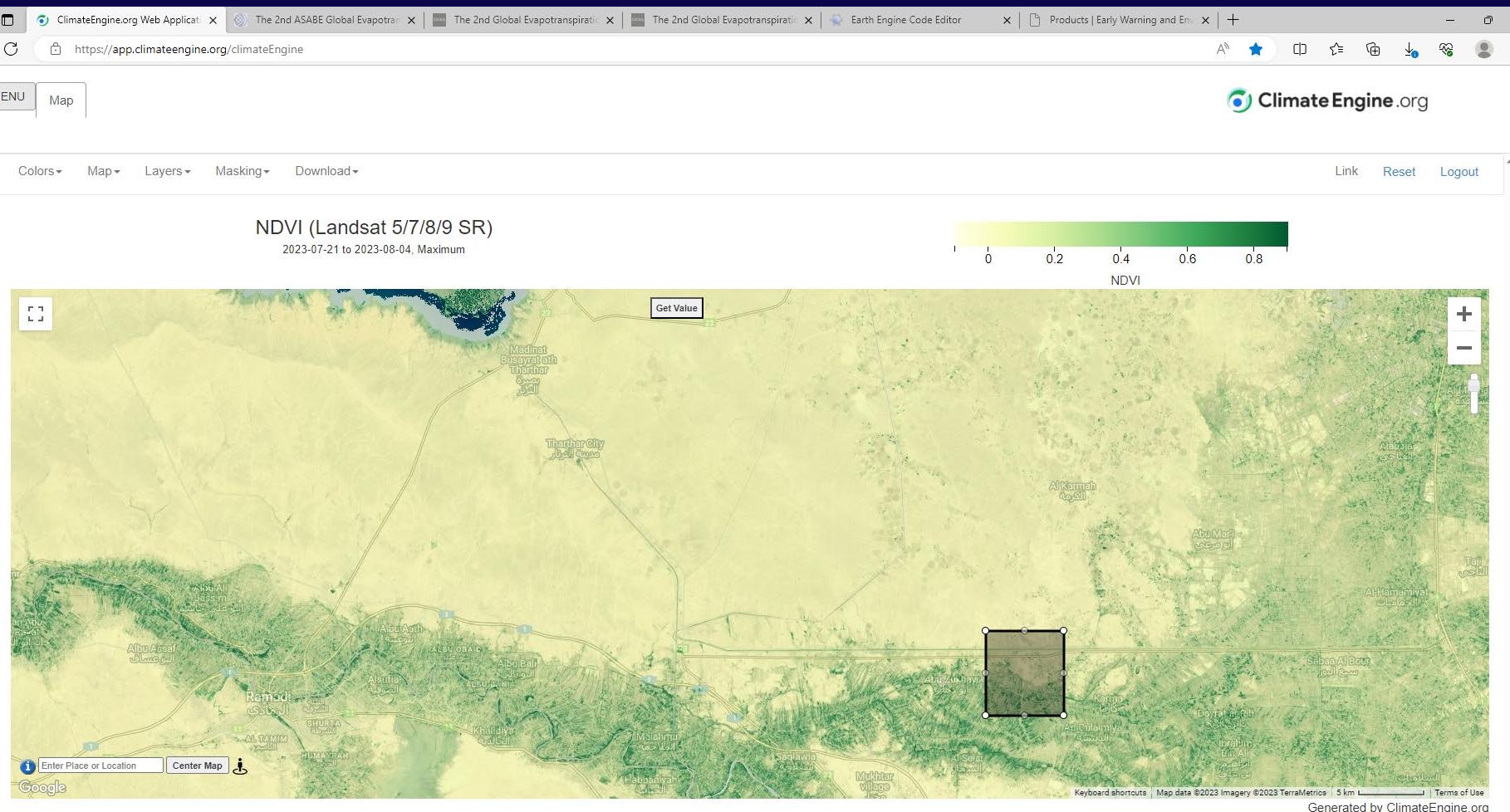
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NDVI 5-km = ~0.3



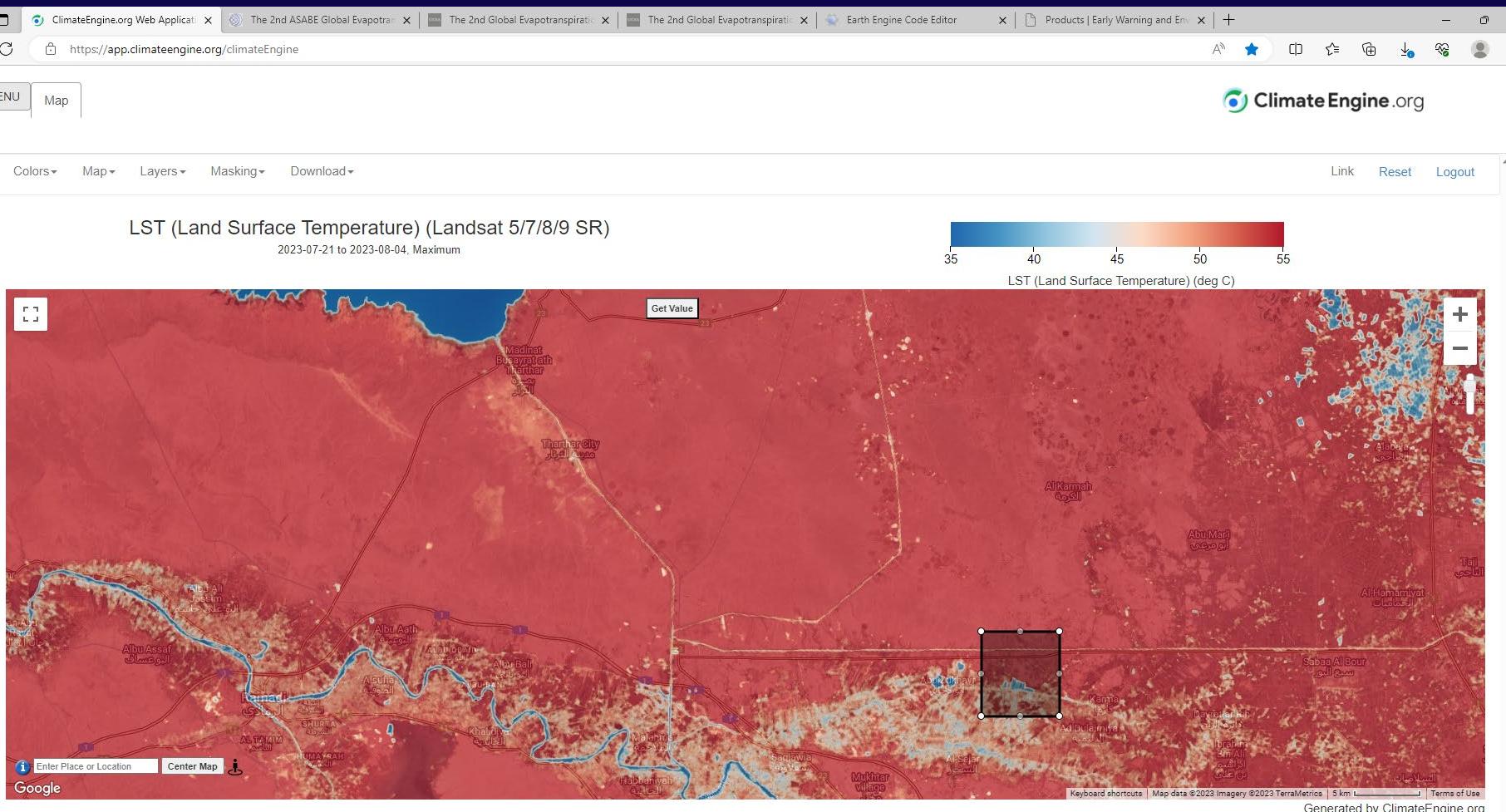
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LST 5-km = ~50 = 323 K



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Sample Calculation:

Assuming

$$dT^* = 20 \text{ K}$$

$$Ts^* = 323 \text{ K}$$

$$NDVI^* = 0.30$$

$$Tc^* = Ts^* - 1.25 * dT (0.9 - NDVI^*)$$

$$Tc^* = 323 - 1.25 * 20(0.9 - 0.3)$$

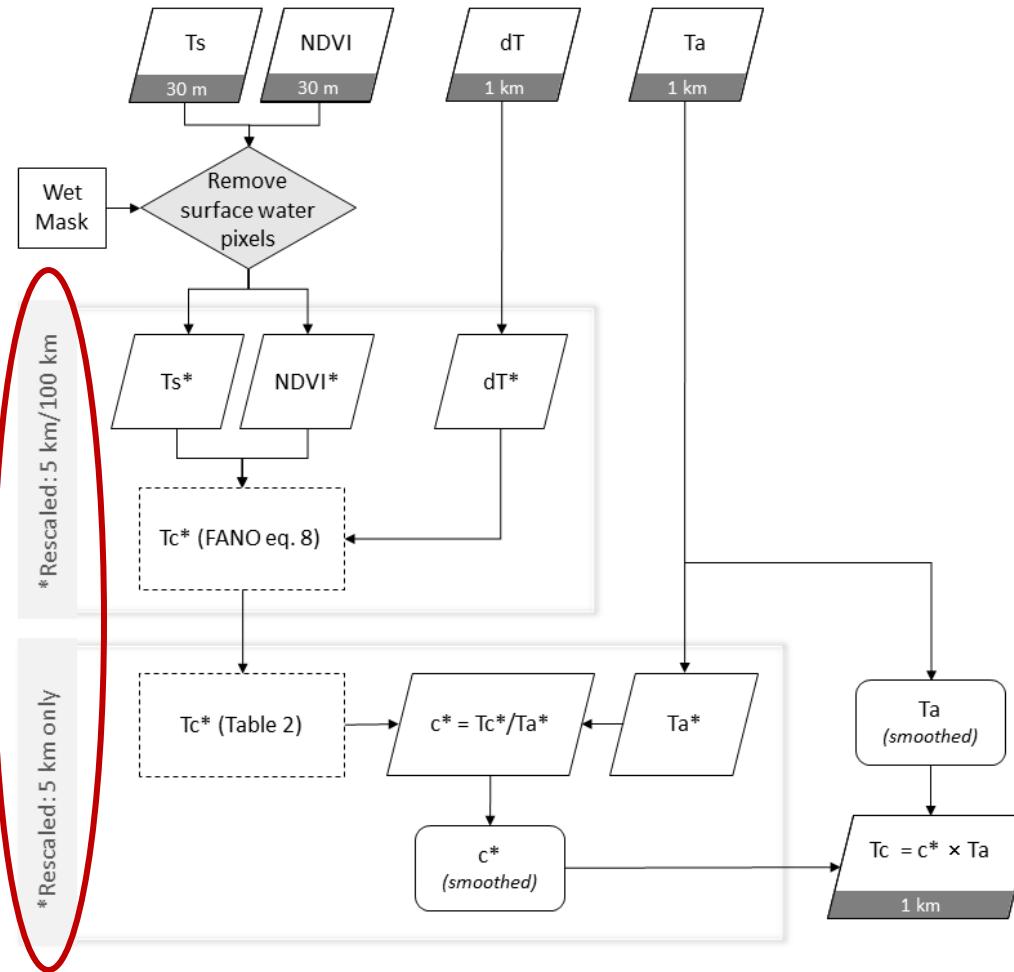
$$Tc^* = 308 \text{ K}$$

$$Tc^* = 35^\circ\text{C} \text{ (which is comparable to the water temp)}$$

TC* is then disaggregated to 1 km to Tc using air temperature (Ta). But Ta does not vary much over flat areas and its effect is limited.

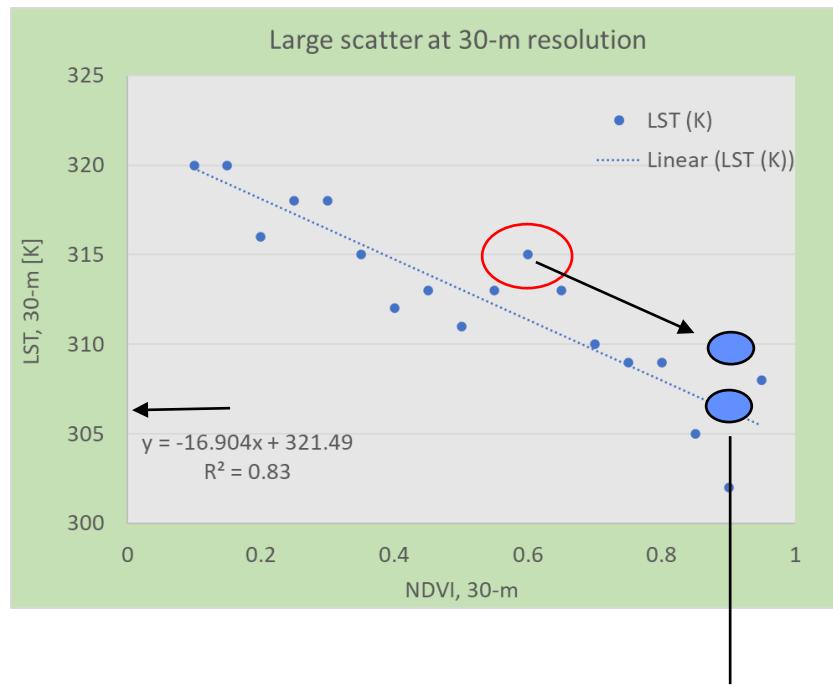


Tc Determination Steps

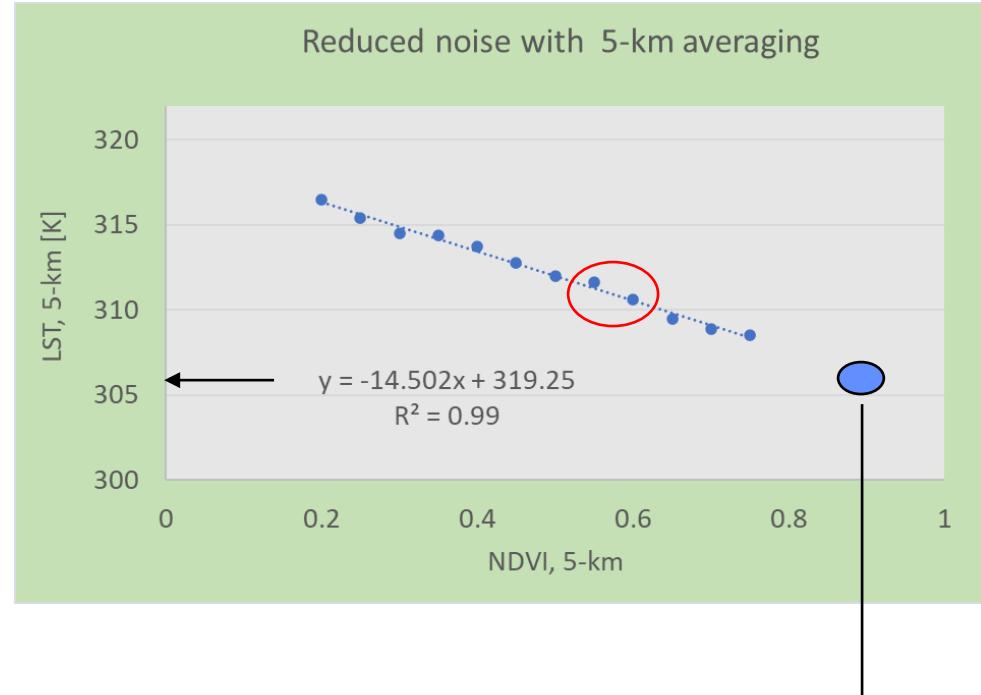


Why 5-km Spatial Averaging? To Reduce Noise

Avoid over- or under-predication of Tc for neighboring pixels.



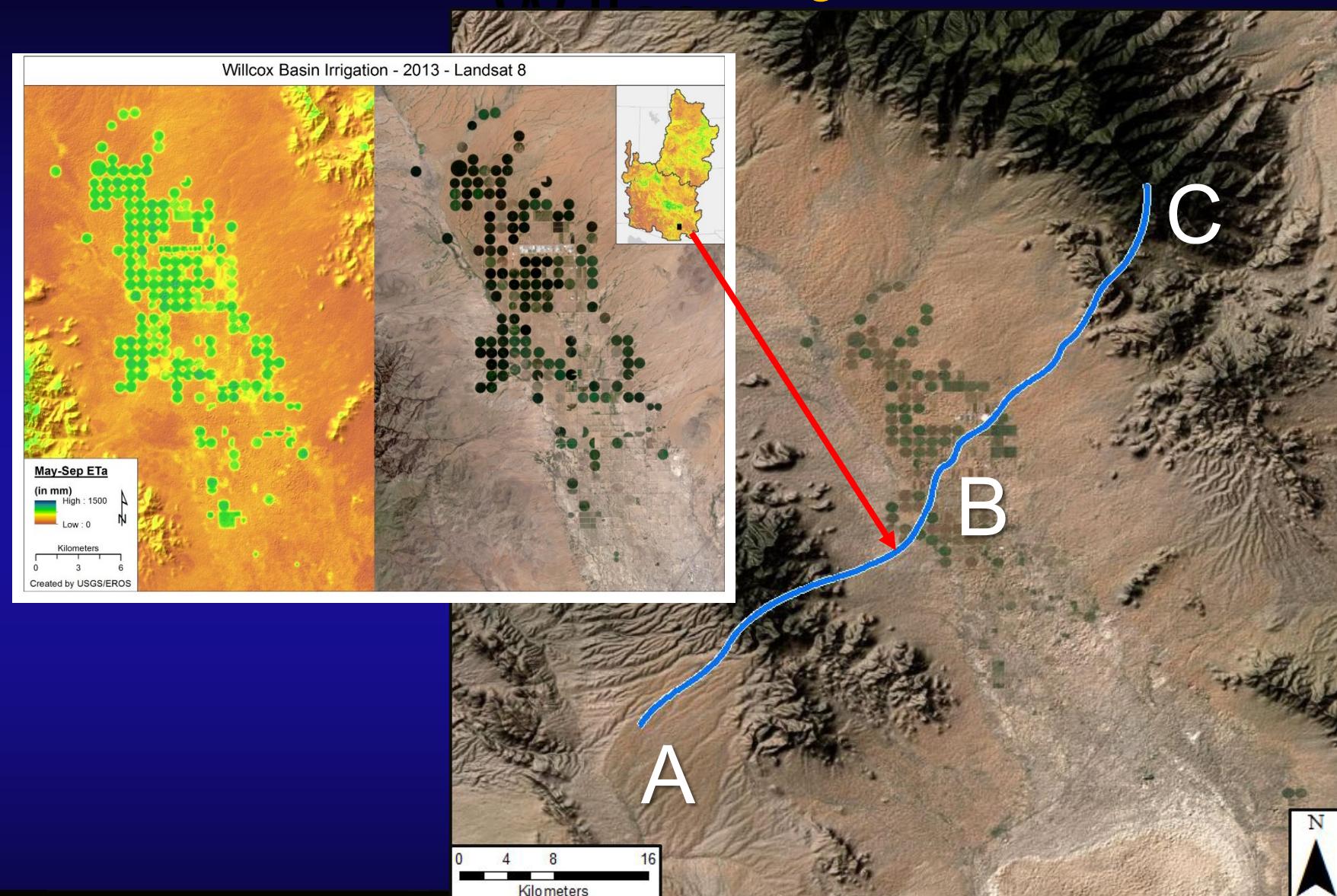
NDVI = 0.90
LST = 306.3 K



NDVI = 0.90
LST = 306.2

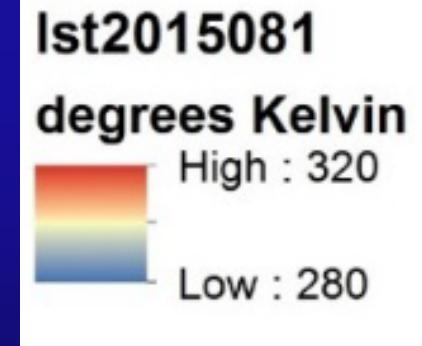
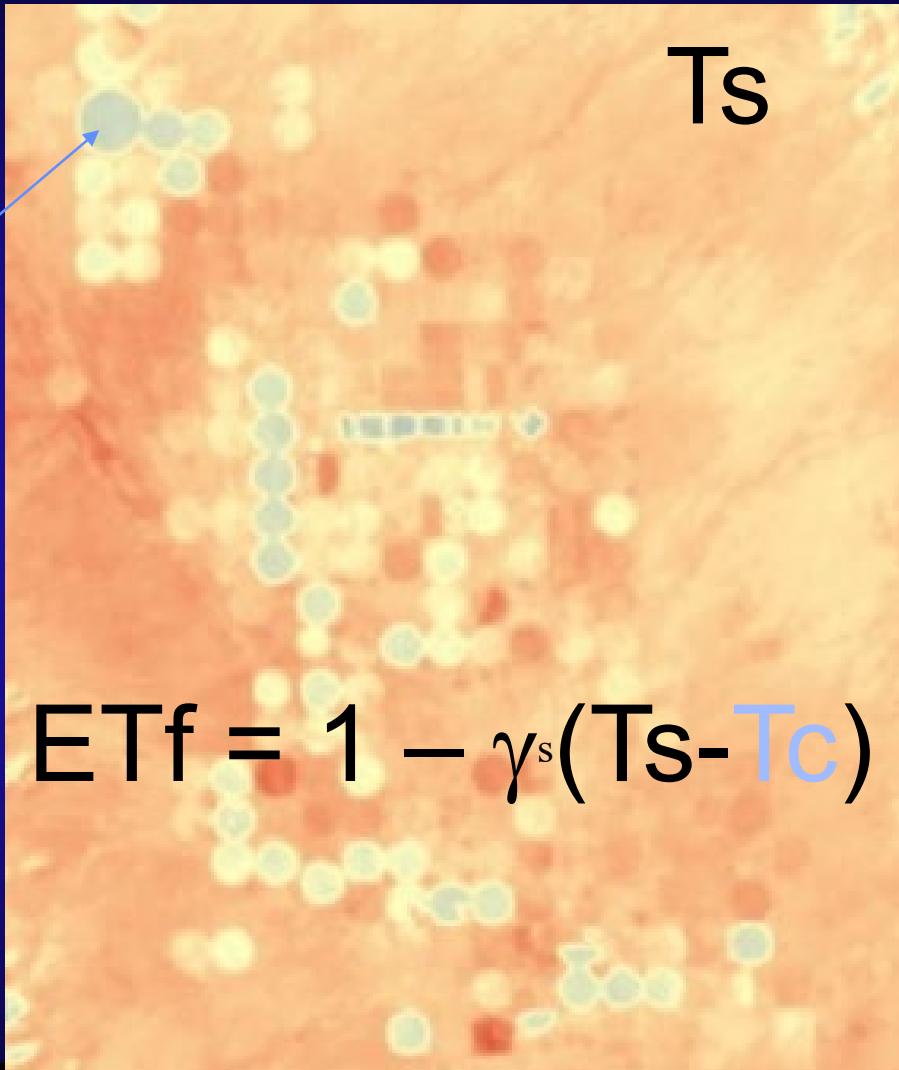


Transect in Willcox Irrigation Basin



LST (Ts) distribution in an irrigated valley Willcox, AZ,: March 21, 2015)

Ts=Tc

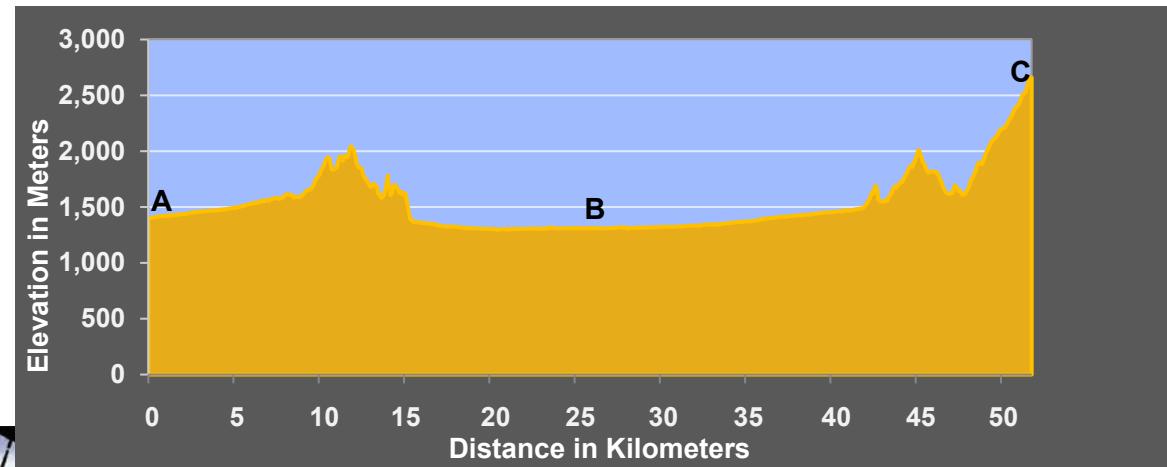
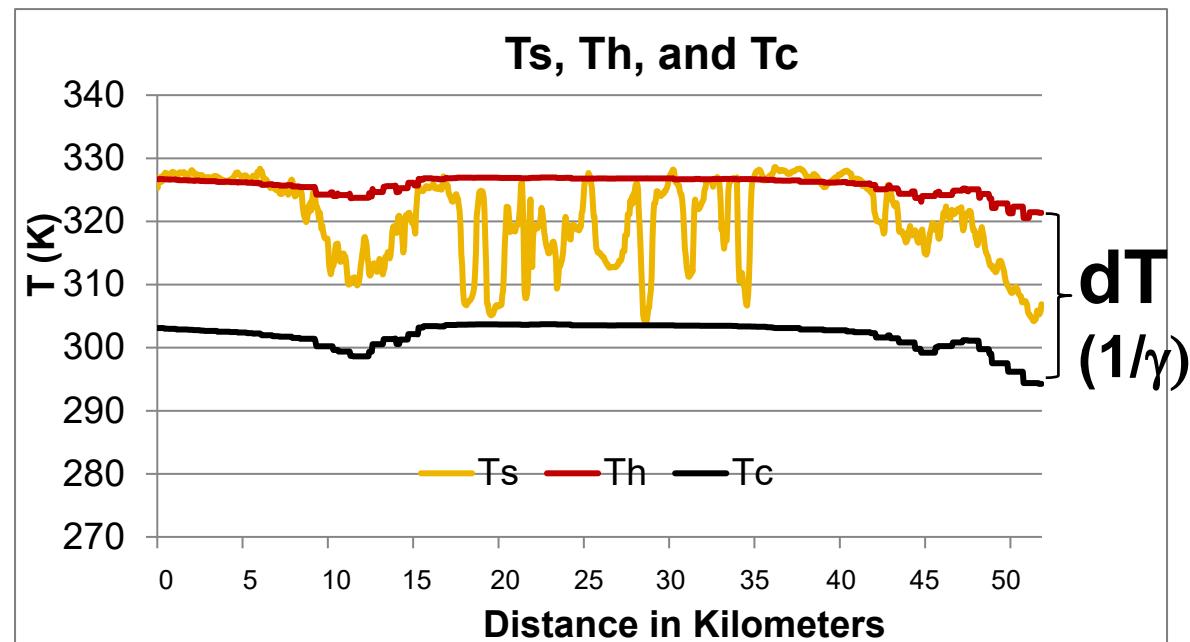
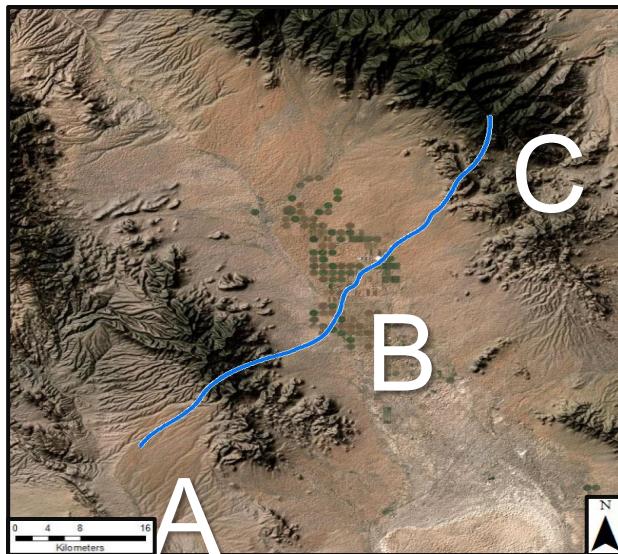


LST(Ts), Hot (Th)/Cold (Tc) Limits for Jun 23, 2014

$$ETf = 1 - \gamma^s (Ts - Tc) \quad (0 - 1)$$

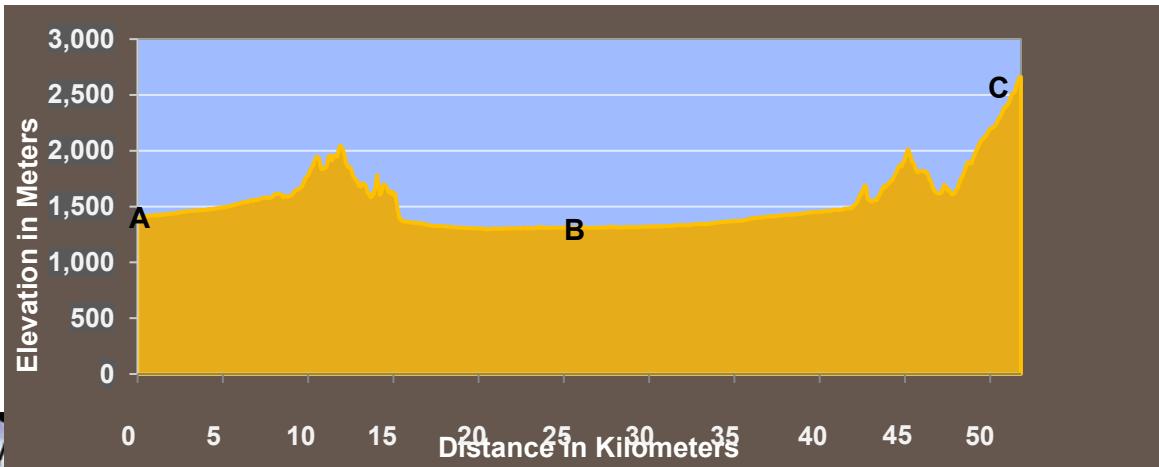
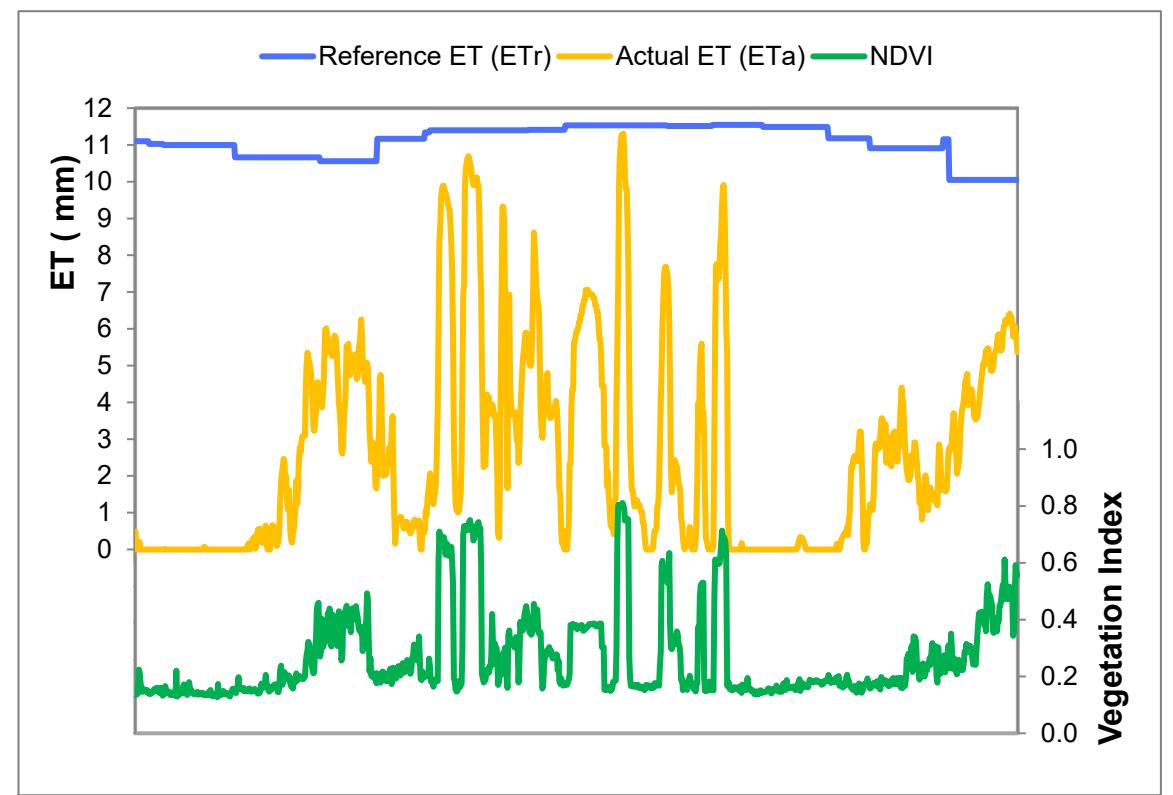
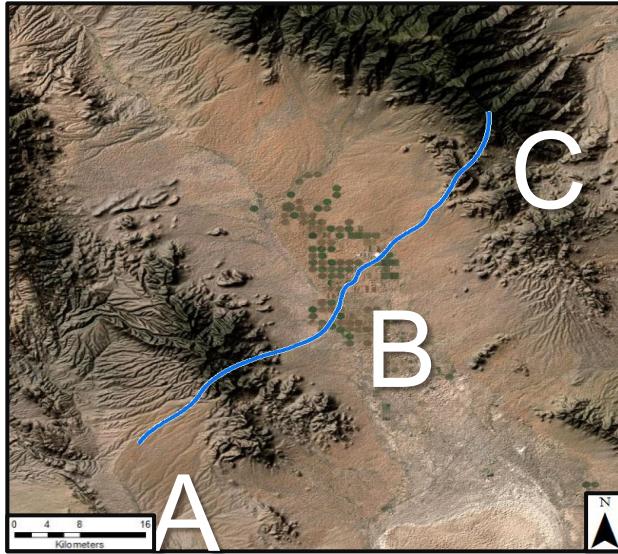
$$\gamma^s = \frac{\rho Cp}{Rn r_a}$$

$$ETa = ETo - \gamma^s (Ts - Tc) ETo$$

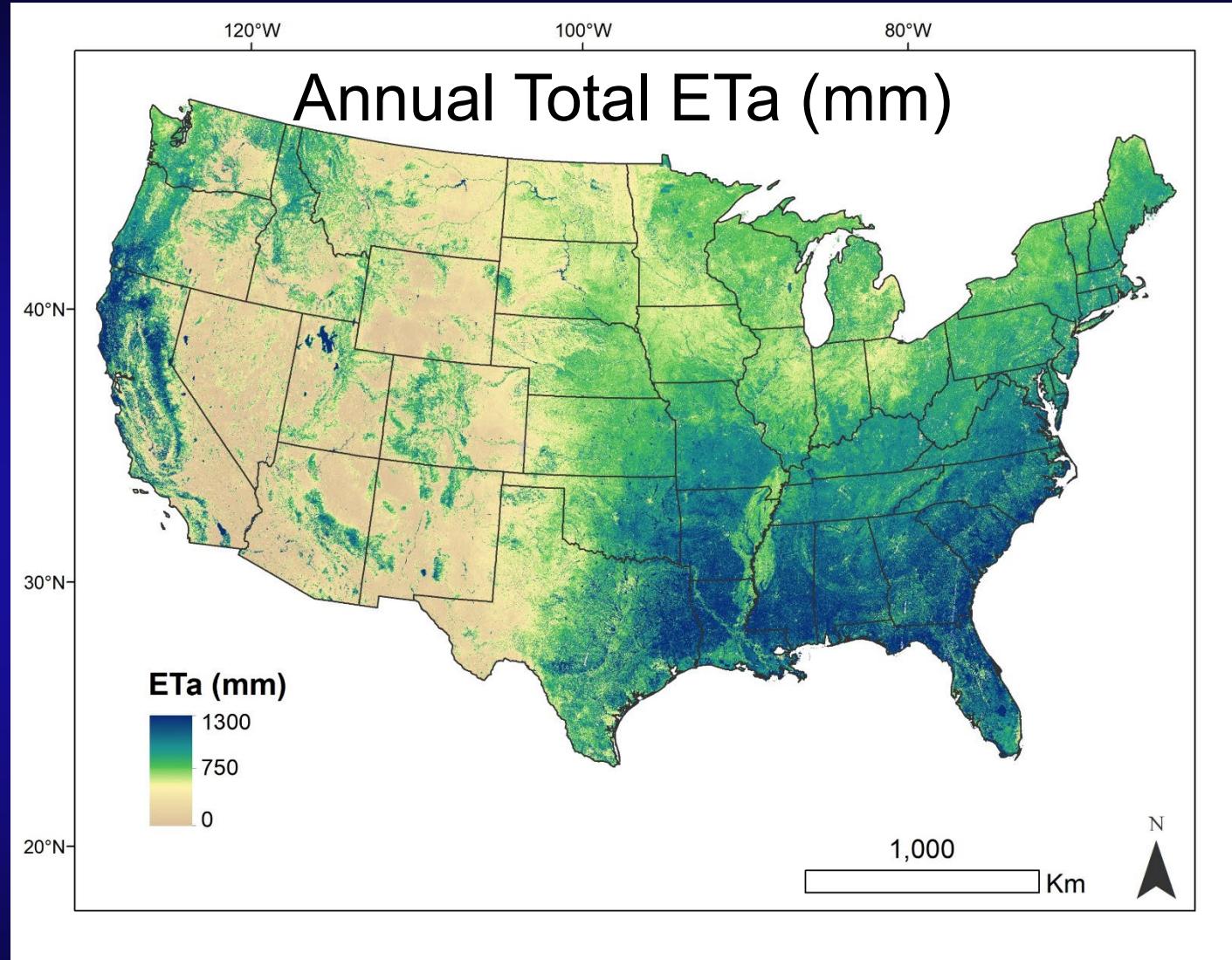


ET_a, PET (ET_r), NDVI

$$ET_a = ET_o - \gamma^s (T_s - T_c) ET_o$$



1st Ever Landsat Scale CONUS ETa



Questions?



Challenge: ET under potential vs water limiting conditions

- Landscape is at different levels of stress; thus, actual ET is \leq potential.
- Allen et al (1998)
 - $ET = K_s * K_c * ETo$
 - K_c = type and stage of crop ($\sim 0.15 - 1.0$)
 - K_s = soil moisture stress factor (0 to 1)

(This requires knowledge of crop types, stage and moisture distribution)



More direct estimation of stress using remote sensing approaches...

Land surface temperature (LST) derived from remotely sensed imagery can be used to estimate the combined effects of soil moisture and environmental stress factors on vegetation.

$$ET = ET_f * ETo$$



$$Ks * Kc$$



Energy Balance Approach for ET:

Accounts for water, agronomic and environmental stresses

USGS WaterSMART and FEWS NET use the SSEBop (Operational Simplified Surface Energy Balance) approach for:

- 1) Water Use and Availability Assessment
- 2) Drought Monitoring & Early Warning

